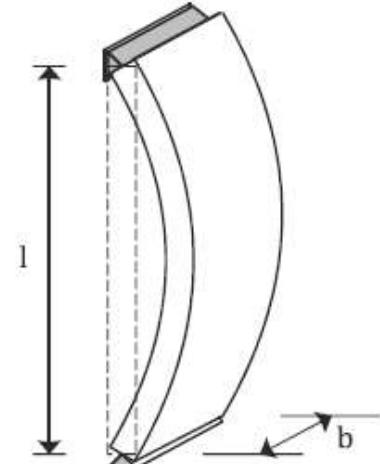
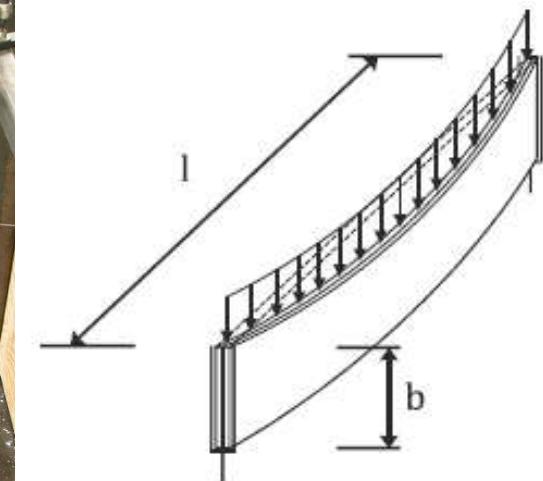


CEN/TS 19100-3  
in-plane loaded elements and joints

## in-plane loaded elements



column buckling



lateral torsional buckling

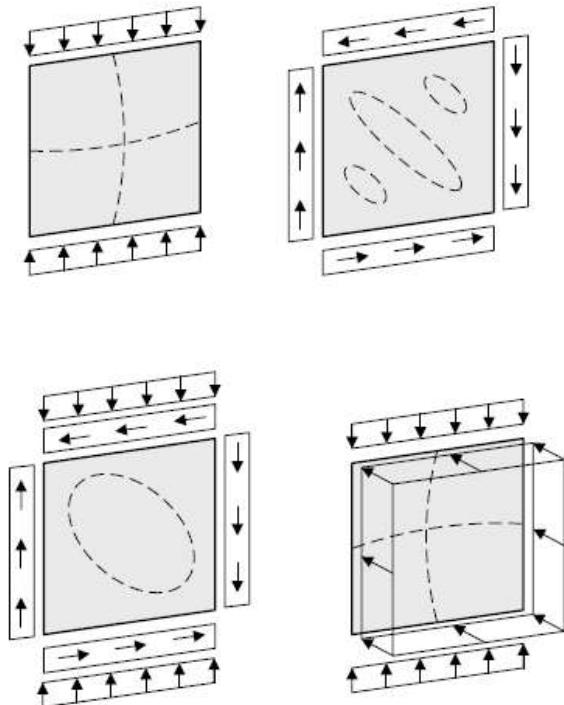
## in-plane loaded elements



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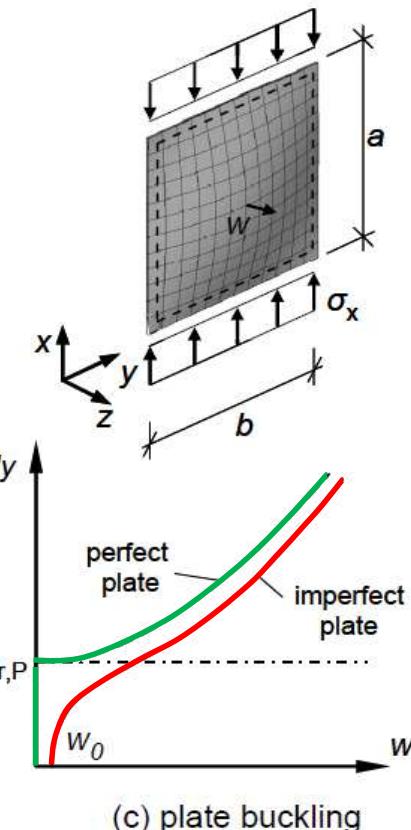
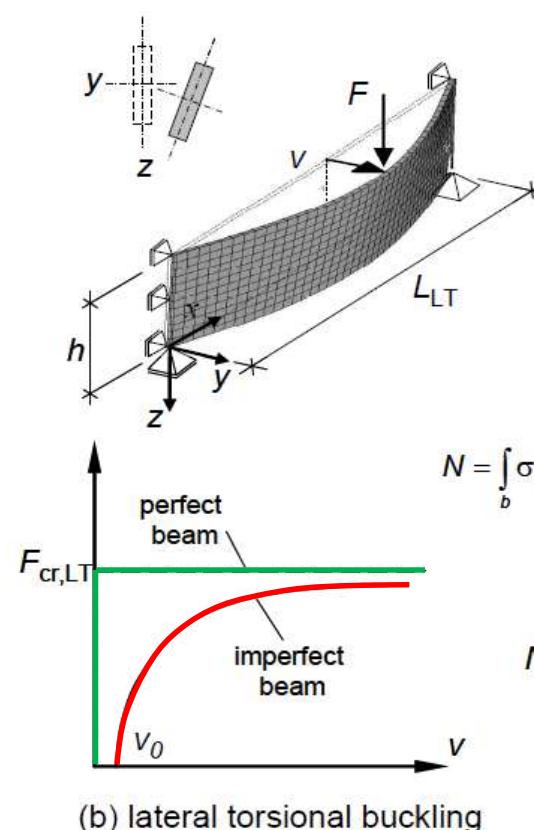
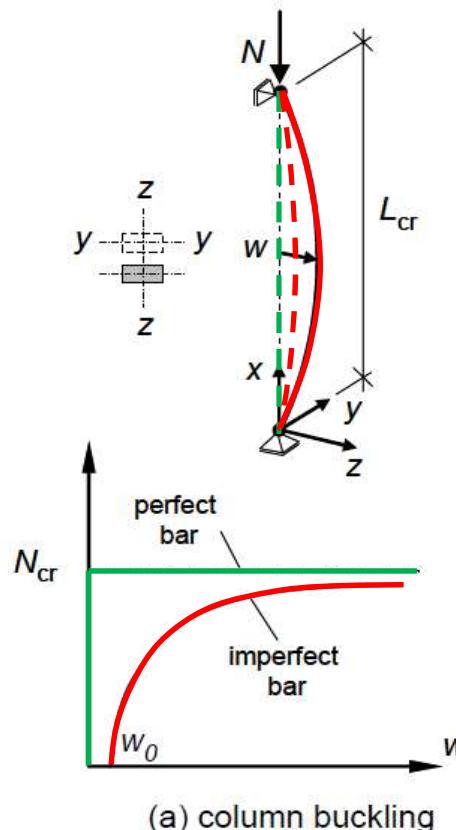


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## plate buckling

## in-plane loaded elements



## in-plane loaded elements

- ✓ structural analysis
  - second order effects

$$\alpha_{cr} = \frac{F_{cr}}{F_{Ed}} \leq 10$$

- imperfections
  - equivalent geometrical imperfection
  - basic imperfection (ULS and SLS)\*

$$e_0 = \sqrt{e_{0,length}^2 + e_{0,installation}^2}$$

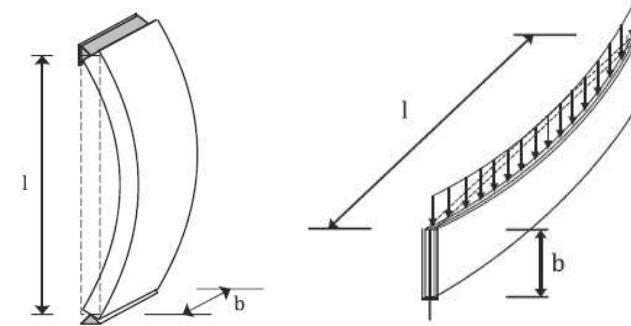


Table 7.1 (NDP) — Imperfection parts for buckling cases

Type	$l_0$	both for mono and laminated glass panes	
		$e_{0,length}^a$	$e_{0,installation}^{b,c,d}$
Flexural buckling and plate buckling	Distance of inflexion points in the relevant critical mode in direction of the applied load	$l_0/333$	$h_e/2$
Lateral torsional buckling	Distance of inflexion points at the edge in compression in the relevant critical mode	$l_0/450$	$h_e/2$
Shear buckling	Longest diagonal	$l_0/1000$	$h_e/5$

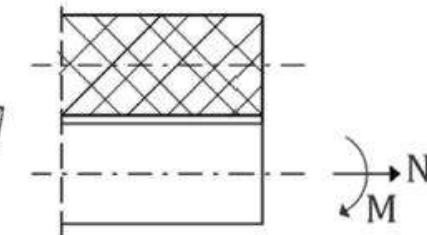
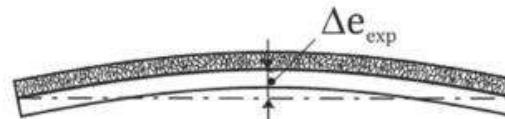
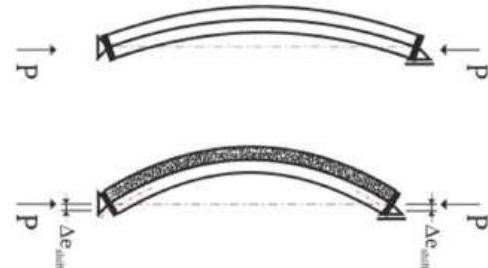
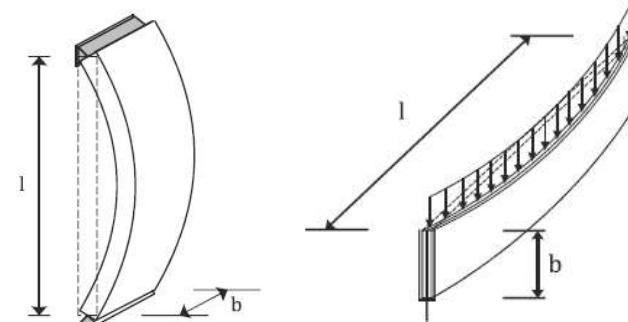
<sup>a</sup>  $e_{0,length}$  should be applied at the location where the curvature of the relevant critical mode gets its maximum.  
<sup>b</sup>  $e_{0,installation}$  may be applied at the location where the installation eccentricity occurs. Alternatively, for simplification reasons, it may be applied at the same location as the one of  $e_{0,length}$ .  
<sup>c</sup> For perpendicular to the glass plane, straight edges over the thickness of the laminate, the value for  $h_e$  is:  $h_e = h_{top}$ . For stepped edges or other edge geometries the value of  $h_e$  can be determined individually.  
<sup>d</sup> If  $e_{0,installation}$  is recorded on site it may be reduced to the measured value, but not smaller than 3mm. This requires care in execution and control.

## in-plane loaded elements

- ✓ structural analysis
  - second order effects

$$\alpha_{cr} = \frac{F_{cr}}{F_{Ed}} \leq 10$$

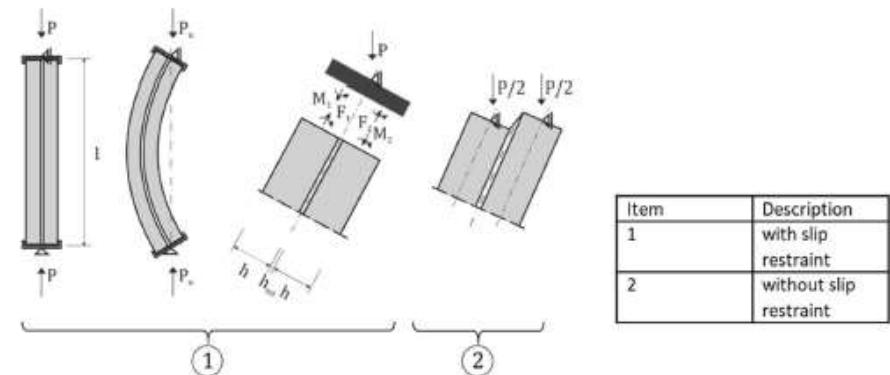
- imperfections
  - equivalent geometrical imperfection
  - basic imperfection (ULS and SLS)\*
  - shift after fracture laminated glass and/or TTG ply



## in-plane loaded elements

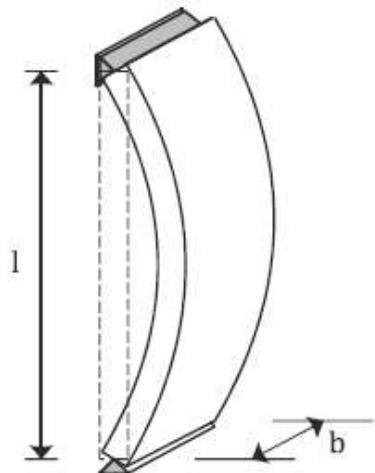
### ✓ points of attention

- interlayer properties (level 0, 1, 2)
- temperature and long-term effects
- detailing
  - load introduction
    - continuous vs concentrated
  - avoid peak stresses
    - durable detailing
  - avoid hard contact
    - deformations
    - tolerances (manufacturing and erecting)
  - slip restraint



in-plane loaded elements

- ✓ critical buckling load  $N_{cr}$



$$N_{cr} = \frac{\pi^2 EI_{z,eff}}{L^2}$$

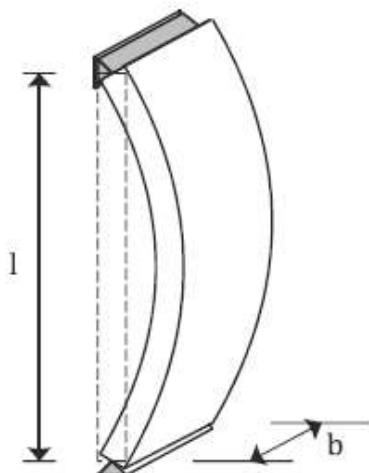
$$I_{z,eff} = \frac{\sum I_i}{1 - \frac{\Psi \cdot \beta \cdot K_s}{\left(\frac{\pi}{L}\right)^2 + \alpha^2}}$$

Table B.1 – Cross section parameters for effective inertia calculation

$K_s$	$\frac{G_L}{t} B$	$\frac{G_L(t)}{t} B$
$\alpha^2$	$\frac{K_s}{E} \left( \frac{(z_1 + z_2)^2}{I_1 + I_2} + \frac{1}{A_1} + \frac{1}{A_2} \right)$	$\frac{K_s}{E} \left( \frac{2(z_1 + z_2)^2}{2I_1 + I_2} + \frac{1}{A_1} \right)$
$\beta$	$\frac{(z_1 + z_2)}{E(I_1 + I_2)}$	$\frac{(z_1 + z_2)}{E(2I_1 + I_2)}$
$\Psi$	$(z_1 + z_2)$	$2 \cdot (z_1 + z_2) = 2 \cdot z$

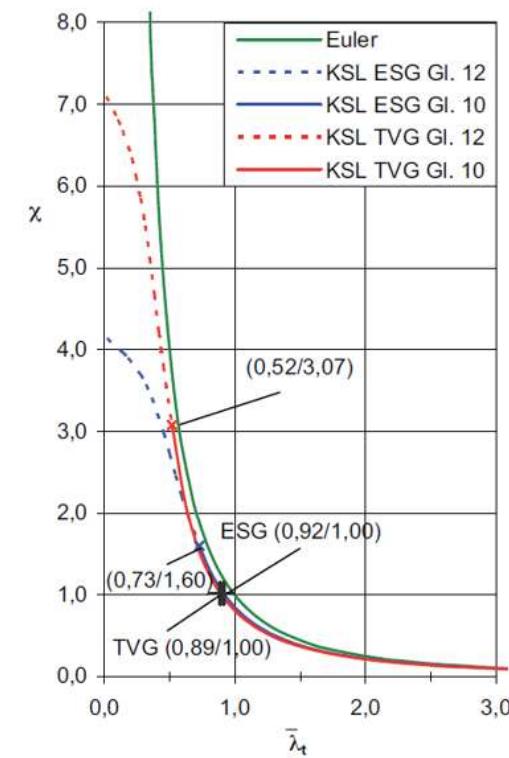
in-plane loaded elements

- ✓ critical buckling load  $N_{cr}$



$$N_{cr} = \frac{\pi^2 EI_{z,eff}}{L^2}$$

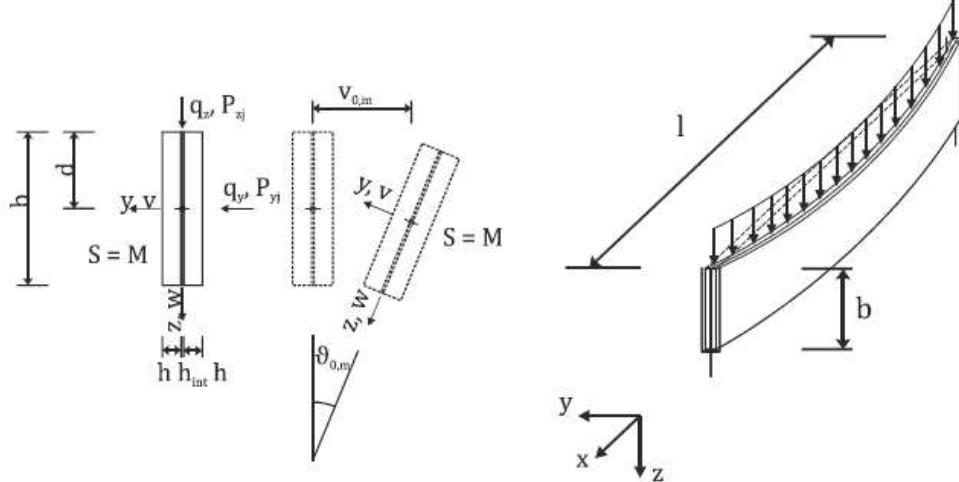
slenderness ratio  $\lambda$   
reduction factor  $\chi = f(\lambda)$   
buckling strength  $N_{b,Rd}$



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## in-plane loaded elements

- ✓ critical bending moment  $M_{cr}$



$$M_{cr,LT} = C_1 \frac{\pi^2 EI_{z,eff}}{L^2} \left[ \sqrt{(C_2 z_p)^2 + \left( \frac{G I_{t,eff} L^2}{\pi^2 EI_{z,eff}} \right)} + (C_2 z_p) \right]$$

Table A.1 — Values  $C_1$  and  $C_2$ 

Bending moment	$C_1$	$C_2$
Constant	1.0	-
Linear (zero at midspan)	2.7	0.0
Parabolic (zero at both extremities)	1.13	0.46
Triangular (zero at both extremities and maximum at mid span)	1.36	0.55

$$I_{T,eff} = \frac{2}{3} B h^3 + 2B h(h_L + h)^2 \left( 1 - \frac{\tanh(\lambda_T \frac{B}{2})}{\lambda_T \frac{B}{2}} \right)$$

$$\lambda_T = \sqrt{\frac{2 G_L}{G h_L h}}$$